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## **Vector fields on 4-manifolds.**

**Definition 1** *The vector field  $X$  on smooth closed manifold  $M^4$  belong to the class  $W(T^2)$  if the set of non-wandering points of  $X$  consist of a disconnected union of embedded 2-tori with have normal hyperbolic structure.*

**Theorem 2** *On  $M^4$  exist vector field  $X$  from  $W(T^2)$  with Lyapunov function  $f$ , who is  $T^2$ -Bott function such that pre-image its any regular point are union 2-torus bundles over circle,if and if  $M^4$  is semi- graph manifold.*

The function  $f$  generates of the Kronrod-Reeb graph  $\Gamma(f)$ . We describe combinatorial conditions of the  $\Gamma(f)$ .

Using classification of Morse functions on surfaces obtained classification  $L$  - equivalent vector fields from  $W(T^2)$  on semi- graph manifold  $M^4$ .

By definition two vector fields  $X$  and  $Y$  are  $L$  - equivalent if they have topological equivalent Lyapunov functions.