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**Algebraic Nijenhuis operators and Kronecker Poisson pencils**

Abstract:

We give a criterion of (micro-)kroneckerity of the linear Poisson pencil on  $\mathfrak{g}^*$  related to an algebraic Nijenhuis operator  $N : \mathfrak{g} \rightarrow \mathfrak{g}$  on a finite-dimensional Lie algebra  $\mathfrak{g}$ . As an application we get a series of examples of completely integrable systems on semisimple Lie algebras related to Borel subalgebras and a new proof of the complete integrability of the free rigid body system on  $\mathfrak{gl}_n$ .